

SAMPL

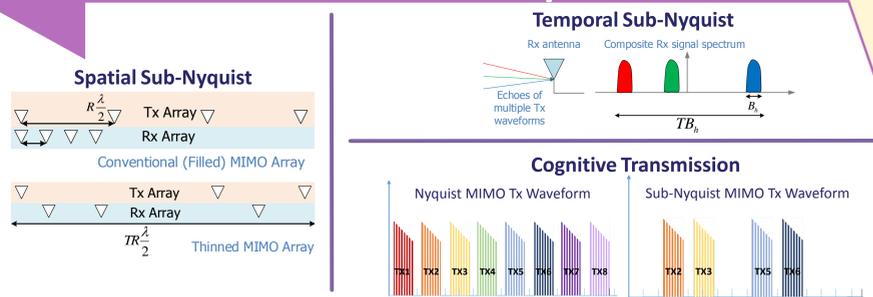
Signal Acquisition Modeling and Processing Lab

Xampling-Enabled Coexistence in Spectrally Crowded Environments

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Cognitive Sub-Nyquist MIMO Radar (SUMMeR)

SUMMeR Concepts



Spatio-Temporal Xampling and Doppler Processing

- Received signal for P pulses at the qth antenna after demodulation:

$$x_q(t) = \sum_{p=1}^P \sum_{m=1}^M \sum_{k=1}^K a_{km} h_m(t - t_k - pt) e^{j2\pi f_{km} t} e^{j2\pi f_d t} e^{j2\pi f_c t}$$
- Fourier coefficients of the mth transmitter channel at the qth receiver:

$$y_{m,q}^p[k] = \sum_{t=1}^L a_{km} e^{j2\pi f_{km} t} e^{-j2\pi f_c t} e^{-j2\pi f_d t} e^{j2\pi f_c t} e^{j2\pi f_d t}$$
- Xampling retrieves the Fourier coefficients from low rate samples
- Doppler focusing for a specific frequency v:

$$\phi_{m,q}^p[k] = \sum_{t=1}^L a_{km} e^{j2\pi f_{km} t} e^{-j2\pi f_c t} e^{-j2\pi f_d t} e^{j2\pi f_c t} e^{j2\pi f_d t} \times \begin{cases} 1 & |f_c^p - v| < 1/2P \\ 0 & \text{else} \end{cases}$$
- Goal: Recover delay, azimuth, Doppler and reflectivity from $\phi_{m,q}^p[k]$
- Fourier coefficients for the mth transmission in matrix form:

$$\mathbf{Z}^m = (\mathbf{B}^m \otimes \mathbf{A}^m) \mathbf{X}_p \mathbf{F}^m$$
- Use OMP for simultaneous sparse 3D recovery with focusing

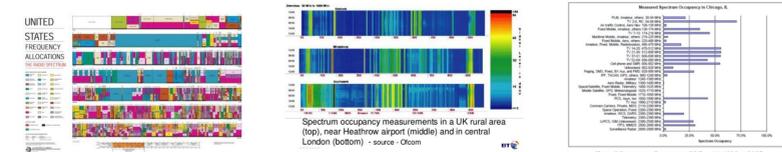
Hardware Prototype and Measurement Results

Sub-Nyquist mode (3) detection performance is same as Nyquist mode (1). Cognitive Sub-Nyquist (3) performs better than Nyquist in low SNR.

Compressed Carrier and Direction-of-arrival Estimation (CaSCADE)

Cognitive Radio (CRo)

- Address the conflict between spectrum saturation and underutilization
- Grant opportunistic access to spectrum "holes" to unlicensed users
- Perform spectrum sensing task efficiently, in real-time and reliably



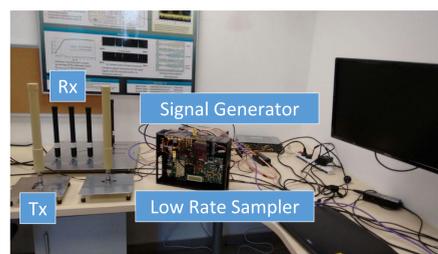
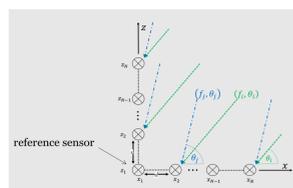
- Nyquist sampling is not an option \Rightarrow sub-Nyquist sampling
- Joint DOA estimation and spectrum sensing increase CR efficiency

Signal Model and Sampling Scheme

- Multiband model: M signals with max. bandwidth B and max. frequency $\frac{f_{Nyq}}{2}$.
- Each transmission $s_i(t)$ is characterized by an angle of arrival (AOA) θ_i and carrier frequency f_i .
- Goal: perfect blind reconstruction of θ_i, f_i and $s_i(t)$
- Relation between known discrete time Fourier transforms (DTFTs) of the samples from the ULA in x axis and unknown signal Fourier transform:

Algorithm, Hardware Prototype and Results

- L-shape ULA with N sensors in x axis and N + 1 sensors in z axis:
- Phase accumulation in x axis: $\Delta\phi_{x_n}(f_i, \theta_i) = \frac{2\pi d}{c} \cdot n \cdot f_i \cos(\theta_i)$
- Phase accumulation in z axis: $\Delta\phi_{z_n}(f_i, \theta_i) = \frac{2\pi d}{c} \cdot n \cdot f_i \sin(\theta_i)$
- Received signal at nth sensor in x axis: $U_n(f) = \sum_{i=1}^M S_i(f - f_i) e^{j\Delta\phi_{x_n}(f_i, \theta_i)}$
- To overcome the pairing problem: Compute cross correlation matrices between ULAs
- Perform joint SVD on the cross-correlations
- Compute θ_i and f_i from the paired eigenvalues



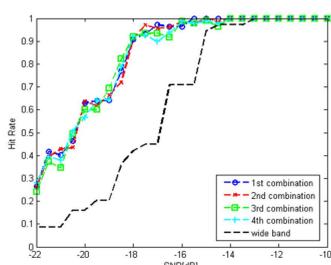
Compared methods:

- PARAFAC: iterative algorithm (based on alternating least squares)
- Compressed sensing (CS): exploiting the spectrum sparsity
- Joint SVD ESPRIT (SVD): analytic solution (as presented)

Spectral Coexistence via Xampling (SpeCX)

Cognitive Radar (CRr)

- Transmitter:
 - Only in the available bands
 - Dynamic changes in frequency bands location
 - Receiver:
 - Sampling only transmitted bands
 - Xampling techniques to accurately detect targets despite low total bandwidth
 - Recovery process: identical
 - Advantages:
 - Reduced transmitted bandwidth: coexistence with communication signals
 - Inherent high SNR system: all the power that was spread along the wideband is now concentrated in the narrow bands
 - Preservation of resolution: Xampling recovery techniques
- By transmitting only the bands to sample, we achieve better performance without trade-off



Spectral Coexistence

- Radio Environment Map (REM) is assumed to be known
- Goal: Select bands with minimal interference
- Finding a block sparse vector
- Known length blocks (receiver passband is known a priori)
- Structured greedy algorithms (StructOMP) for recovery

- Comm systems can share the unused cognitive radar transmit spectrum
- Recovery for CRo and CRr signals is via Xampling
- Spectral coexistence without loss of range resolution in CR
- CS-based blind sensing in CRo

Hardware Prototype and Measurement Results

